On-Chip Multiplication Gain

In order to gain a clearer understanding of biological processes at the single-molecule level, a growing number of experiments are being conducted using small-volume samples. Both the lower fluorophore concentrations and the faster kinetics associated with these experiments establish a key criteria for choosing an appropriate camera system.

This technical note endeavors to provide a comprehensive look at the advantages and limitations of *on-chip multiplication gain*, a new CCD technology designed for low-light, high-speed imaging.

The following topics are discussed:

• **Low-light, high-speed challenges**

• **Applicable popular technologies**

• **On-chip multiplication gain**

Imaging at Low Light Levels

Requirements

CCD performance has improved significantly through the years. Reductions in read noise and increases in quantum efficiency (QE) have served to lower the detection limits of leading-edge imaging systems. For example, Photometrics® offers back-illuminated CCD cameras that boast QE greater than 90% and read noise as low as 2 e- rms (see **Figure 1**).
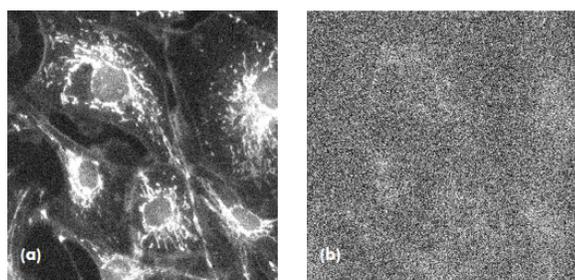

Figure 1. Low-light sensitivity (a) increases with low read noise and (b) decreases with high read noise.

However, the best read-noise performance is attainable only when readout speed is reduced considerably (i.e., into the range of "a fraction of a frame" to "a few frames" per second). Thus, traditional low-light-level imaging systems face a fundamental challenge when they are required to capture low-light events at video frame rates and faster.

> **FACT** CCD read noise increases as readout speed increases.

Intensified CCDs

In order to overcome the limitation on sensitivity imposed by read noise at higher speeds, the signal itself is often amplified above the read noise. Photomultiplier tubes were among the first to implement this strategy.

> **FACT** Amplifying the incoming signal effectively reduces the input-referenced read noise.

Today, image intensifiers are frequently employed for low-light-level imaging. In an intensified CCD (ICCD) camera system, incoming photons are multiplied by the image intensifier and subsequently detected by a traditional CCD.

ICCD camera systems offer a proven solution for applications such as single-molecule fluorescence (SMF), a type of live-cell imaging that demands very high detector sensitivity along with readout rates equal to and beyond those associated with video. However, while vast improvements have been made to these vacuum devices in terms of sensitivity and resolution over the years, they still suffer from a few disadvantages, including susceptibility to damage under high-light-level conditions as well as lower spatial resolution.

> **ICCD PROS** Good low-light-level sensitivity and the ability to act as a fast shutter (psec or nsec gating)

> **ICCD CONS** Susceptibility to damage, lower spatial resolution, high background noise

As with ICCDs, electron-bombardment CCD (EBCCD) camera systems use a photocathode to convert incoming photons to electrons; the charge is then amplified and detected by a CCD. The technology also carries similar lifetime, resolution, and background-noise limitations.
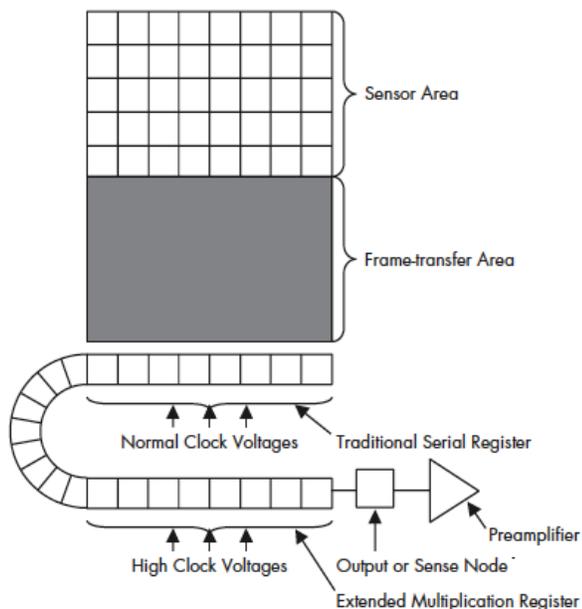

Figure 2. This example of an electron-multiplying CCD has a frame-transfer architecture.

On-chip Multiplication Gain

High Performance in Low Light

Recently, CCD manufacturers have introduced novel, high-sensitivity CCDs engineered to address the challenges of ultra-low-light imaging applications – without the use of external image intensifiers. The new detectors utilize revolutionary *on-chip multiplication gain* technology to multiply photon-generated charge above the read noise, even at supravideo frame rates.

This special, signal-boosting process occurs before the charge reaches the on-chip readout amplifier, effectively reducing the CCD read noise by the on-chip multiplication gain factor, which can be greater than 1000x. The main benefit of the technology, therefore, is a far better signal-to-noise ratio for signal levels below the CCD read-noise floor.

The principal difference between a charge-multiplying CCD and a traditional CCD is the presence of a special extended serial register, known as a *multiplication* register, in the new device (see Figure 2). Note that since the on-chip multiplication gain takes place after photons have been detected in the device's active area, it is possible to adapt the new technology to all current CCD formats and architectures. Recently, for example, cameras utilizing back-illuminated versions of these new charge-multiplying CCDs have been introduced (e.g., the Photometrics® Cascade 512B).

Electrons are accelerated from pixel to pixel in the multiplication register by applying higher-than-typical CCD clock voltages (up to 50 V). Secondary electrons are generated via an impact-ionization process that is initiated and sustained when these voltages are applied. The on-chip multiplication gain can be controlled by increasing or decreasing the clock voltages; the resultant gain is exponentially proportional to the voltage.

> **FACT** On-chip multiplication gain is achieved by generating secondary electrons via impact ionization.

Technology Description

As mentioned earlier, the gain factor achieved via the impact-ionization process can be greater than 1000x. In fact, on-chip multiplication gain is actually a complex function of the probability of secondary-electron generation and the number of pixels in the multiplication register.

Mathematically, it is given by

$$G = (1+g)^N$$

where N is the number of pixels in the multiplication register and g is the probability of generating a secondary electron. The probability of secondary-electron generation, which is dependent on the voltage levels of the serial clock and the temperature of the CCD, typically ranges from 0.01 to 0.016. Although this probability is low, the total gain can actually be quite high, owing to a large number of pixels in the multiplication register. For example, a CCD with pixels N equal to 400 and probability g equal to 0.012 produces on-chip multiplication gain G of 118.

> **FACT** On-chip multiplication gain has an exponential relationship to the CCD's high-voltage serial clock.
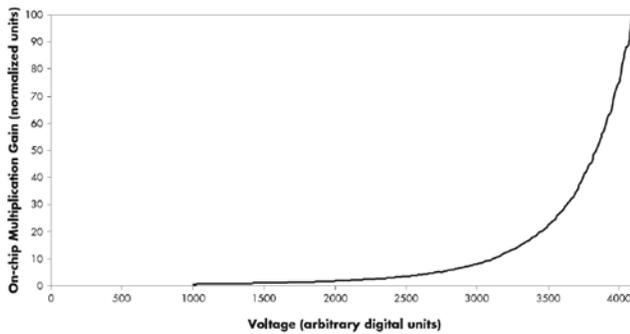
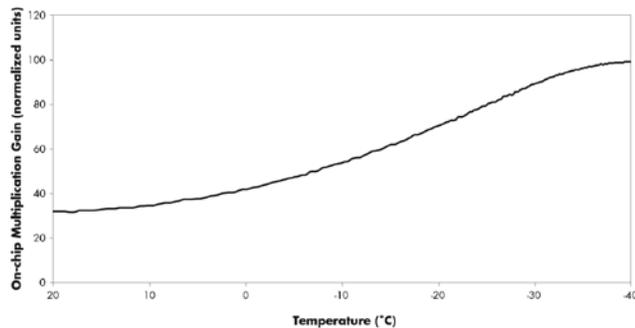**Figure 3.** On-chip Multiplication Gain vs. Voltage

Figure 4. On-chip Multiplication Gain vs. Temperature

Figure 3 clearly illustrates that the "last few volts" of the applied voltage result in a large increase in the on-chip multiplication gain. In practice, the level of voltage is commonly mapped to a high-resolution DAC (digital-to-analog converter) and controlled through software.

Effects of CCD Cooling

Another factor that influences on-chip multiplication gain is the CCD temperature. Simply put, the colder the temperature, the more likely it is for a primary electron to generate a secondary electron in the silicon, resulting in higher on-chip multiplication gain (see Figure 4).

Studies show that greater than 1000x on-chip multiplication gain can be achieved by cooling the detector to -30°C or below. This strong performance dependency underscores the importance of selecting the optimum CCD temperature and preventing its fluctuation with the environment.

As with traditional detectors, cooling a CCD that utilizes on-chip multiplication gain reduces the dark current generated in the pixels of the device. However, for a CCD that utilizes on-chip multiplication gain, it is even more important that dark current be minimized, since this unwanted contributor to system noise is multiplied in conjunction with the desirable, photon-generated signal via impact ionization.

Although cooling the CCD is often beneficial, it can also increase the occurrence of a lesser-known phenomenon called *spurious charge*.

> **FACT** Cooling reduces dark current, increases on-chip multiplication gain, and increases spurious charges.

Spurious charge

When electrons are clocked (moved) through the multiplication register's pixels, the sharp inflections in the clock waveform occasionally produce a secondary electron even if no primary electron is present. As noted previously, this phenomenon, called *spurious charge*, increases slightly as temperature decreases. Exposure time has no effect on spurious charge.

It has been observed that a single spurious electron is generated for every 10 pixel transfers, thus yielding a value of 0.1 e-/pixel/frame. Typically, the spurious-charge component is added to the dark charge in order to determine the total dark-related signal. For example, a CCD camera cooled to -30°C with a dark-current rate of 1.0 e-/pixel/sec (i.e., 0.033 e- per pixel per 30-msec frame) will have dark-related signal of 0.133 e-/pixel/frame.

> **FACT** Total dark-related signal equals spurious charge plus dark charge.

Excess Noise Factor

On-chip multiplication gain is a probabilistic phenomenon, meaning there is a statistical variation in the gain (often, the reported on-chip multiplication gain is en ensemble average). The deviation or uncertainty in on-chip multiplication gain, which is related to the pulse-height distribution found in various scientific literature, introduces some amount of additional system noise, quantified by the *excess noise factor* (F).

Extensive investigations have been conducted in this subject area. Experimental results show that the excess noise factor is between 1.0 and 1.4 for levels of on-chip multiplication gain as high as 1000x. (When calculating total system noise, both the dark- and photon-generated signals are multiplied by the factor F to account for excess noise.)

> **FACT**   The excess noise factor is between 1.0 and 1.4 for on-chip multiplication gain as high as 1000x.

Signal-to-Noise Ratio

A complete derivation of signal-to-noise ratio (SNR) is given in the Appendix. Simply expressed, the signal-to-noise ratio of a CCD with on-chip multiplication is given by

$$SNR_{Total} = (S*QE)/\sigma_{Total}$$

where

S   = total number of photons arriving at each pixel

QE = fraction of photons detected

σ_{Total} = total noise in system =

$$\sqrt{[(S*QE*F^2)+(D*\ F^2)+(\sigma_R/G)^2]}$$

where

D = total dark-related signal (including spurious charge)

F = excess noise factor (typically between 1.0 and 1.4)

σ_R = read noise of detector

G = on-chip multiplication gain factor

The first, second, and third terms of the denominator denote the effective photon (shot) noise, dark noise, and read noise, respectively, as a result of on-chip multiplication gain. Notice that the shot noise and dark noise are both increased by the excess noise factor, whereas the read noise is reduced by the on-chip multiplication gain factor.

Dual Amplifiers

One of the common limitations of cameras designed for low-light imaging is their inability to capture both bright and dim signals in the same frame (owing to a relatively narrow dynamic range). Although these low-light-level CCD cameras can be operated at unity gain for wide-dynamic-range applications, they are still unable to match the dynamic-range capabilities of traditional CCDs.

In CCDs with on-chip multiplication gain, this shortcoming stems from the fact that the readout amplifier (responsible for read noise) associated with the multiplication register is usually designed to run at higher speeds, resulting in higher read noise. Although on-chip multiplication gain easily overcomes the elevated read noise, the dynamic range of the camera system suffers.

To preserve dynamic range, some CCD cameras with on-chip multiplication gain (e.g., the Photometrics Cascade:512F) now feature a dual-amplifier design that incorporates a second, "traditional" amplifier for slower pixel readout. Thus, these high-performance CCD cameras can also be used for wide-dynamic-range applications like brightfield or fluorescence imaging (see Figure 5).
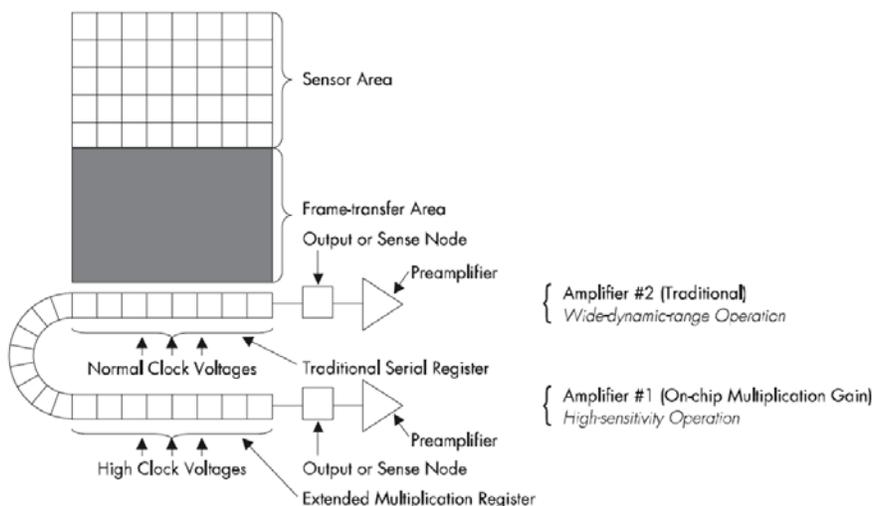

Figure 5. A second, "traditional" readout amplifier makes the Cascade 512F (and Cascade 512B) more versatile by enabling the camera to be used for wide-dynamic-range applications.

Back Illumination

On-chip multiplication gain is also being implemented in back-illuminated CCD architectures. As mentioned previously, back illumination offers greater than 90% QE, effectively compounding the sensitivity advantage provided by charge-multiplying CCDs. This technology tandem delivers the best available low-light-level sensitivity at fast frame rates. Some back-illuminated, charge-multiplying CCD cameras (e.g., the Photometrics Cascade 512B) can be configured with dual amplifiers for broader application versatility.
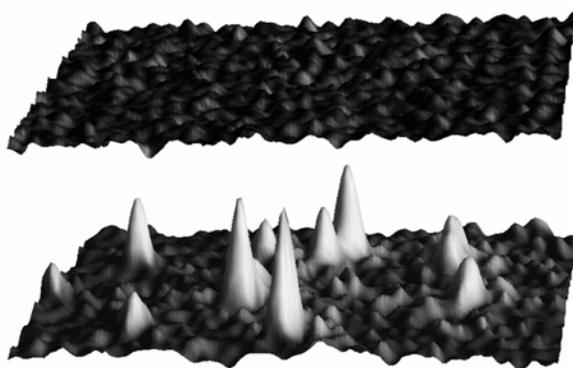

Figure 6. Single molecules of perylene diimide in polymethylmethacrylate gel. Fluorescence emission acquired using a Photometrics Cascade® camera with "on-chip multiplication gain" off (top) and on (bottom). SMF images courtesy of Kallie Willets and Stefanie Nishimura, W.E. Moerner Lab, Department of Chemistry, Stanford University.

Technology Summary

Making an Informed Choice

Much of the sensitivity advantage offered by traditional, cooled CCD cameras comes from their ability to integrate signal on the chip prior to readout and thereby only incur read noise once during measurement. Hence, for the long exposures required in many low-light-level applications, frame rates for these cameras are low.

However, because on-chip multiplication gain overcomes read noise, images can be acquired at faster frame rates with devices that feature the on-chip technology. This capability greatly improves the utility of the new detectors for low-light-level work.

The net result is that devices with on-chip multiplication gain boast the sensitivity of intensified and electron-bombardment CCDs, but don't carry the risk of potential damage to external image-intensifier hardware. And because no photocathode or phosphor is involved, the spatial resolution provided is as high as that offered by traditional CCD imagers with the same array and pixel size.

When properly integrated in a high-performance camera platform, the new CCDs provide researchers an excellent choice for nongated, low-light-level applications that require video (or supravideo) frame rates and excellent spatial resolution. Examples of such applications are intracellular ion imaging, biological fluid flow measurements, and SMF imaging (see Figure 6). When the new detectors are deeply cooled, with on-chip multiplication gain sufficiently higher than the read noise and a low photon-arrival rate, even photon counting should be possible without image-intensifier hardware.

The latest front- and back-illuminated CCD cameras with on-chip multiplication gain feature dual amplifiers in order to ensure the highest level of performance not only for ultra-low-light imaging, but for wide-dynamic-range applications. Now, a single CCD camera can be used for SMF *and* brightfield/fluorescence imaging.

Appendix

Derivation of Signal-to-Noise Ratio
(for CCDs utilizing on-chip multiplication gain)

Signal Calculation

(1)	Number of incident photons at each pixel	S	
(2)	Number of photoelectrons generated in each pixel	$S*QE$	QE is the quantum efficiency at the wavelength of the photons.
(3)	Number of electrons after the on-chip multiplication gain (S_{Total})	$S*QE*G$	G is the on-chip multiplication gain factor.

Noise Calculation

(4)	Photon (shot) noise	$G*F*\sqrt{(S*QE)}$	Incoming photons follow Poisson statistics and have an inherent noise called photon (shot) noise, which is given by the square root of the signal.
			In CCDs featuring on-chip multiplication gain, both the signal and the noise are multiplied by the gain factor (G).
			In addition, the shot noise is multiplied by the excess noise factor (F).
(5)	Dark noise	$G*F*\sqrt{D}$	Total dark-related signal (D) includes dark chare and spurious charge.
			Similar to shot noise, dark noise is given by the square root of total dark-related signal (D).
			Since dark charge also goes through the multiplication process, both the on-chip multiplication gain and excess noise factors are applied.
(6)	Read noise	σ_R	Since read noise occurs after on-chip multiplication gain, it is not affected by on-chip multiplication gain.
(7)	Total system noise (σ_{Total})	$\sqrt{[(G^2*F^2*S*QE)+(G^2*F^2*D)+\sigma_R^2]}$	To derive the total system noise (σ_{Total}), the individual noise components in **(4)**, **(5)**, and **(6)** are added in quadrature (i.e., square the individual components, add, and take a square root of the total)

Signal-to-Noise Ratio

SNR (S_{Total}/σ_{Total})	$S*QE*G /\sqrt{[(G^2*F^2*S*QE)+(G^2*F^2*D)+\sigma_R^2]}$	**(3) / (7)**
	$= (S*QE) /\sqrt{[(S*QE*F^2)+(D*F^2)+(\sigma_R/G)^2]}$	Divide the numerator and denominator by G.

The first and second terms in the denominator of the final equation show that the shot noise and the dark noise are increased due to the excess noise of the charge-multiplying process, whereas the third term (read noise) is effectively reduced by the on-chip multiplication gain factor.

SNR Calculation

The following example illustrates the effect of on-chip multiplication gain on the overall system SNR for various incident-signal levels (i.e., for various numbers of incident photons).

Camera parameters used for this calculation:

Quantum efficiency
@ 600 nm (QE)   = 40%

Read noise (σ_R)   = 60 e- rms

Exposure time   = 33 msec (30 frames/sec)

Dark charge
(dependent on   = 1 e-/pixel/sec @ -30°C
exposure time)   (0.033 e-/pixel/frame)

Spurious charge   = 0.1 e-/pixel/frame

Total dark-related
signal (D)   = 0.133 e-/pixel/frame

Excess noise
factor (F)   = 1.2

The signal-to-noise ratio at each signal level has been computed based on the equation derived earlier and then plotted in the graph. For comparison purposes, the SNR obtained with a similar – but traditional – slow-scan CCD is also presented.

The data indicates:

• CCDs with on-chip multiplication gain offer the greatest advantage at low light levels where the read noise of the CCD is the dominant factor (i.e., in the read-noise-dominant regime).

• On-chip multiplication gain is useful only up to the point of overcoming the read noise. In this particular example, there is very little difference between SNR performance at 200x and 1000x.

• Traditional slow-scan CCDs with sufficiently low read noise achieve better SNR in the shot-noise-dominant regime (i.e., at higher light levels). Thus, there is a distinct advantage in having a single camera with two readout amplifiers – one (on-chip multiplication gain) designed for ultra-low-light imaging and another (traditional) that offers better support for wide-dynamic-range applications.
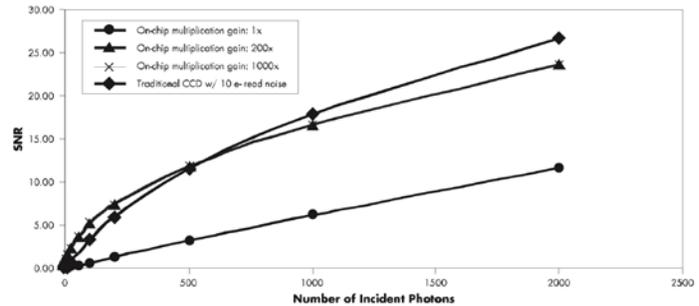
By changing the QE in this example to 90% (or greater), it's easy to see that a back-illuminated version of a charge-multiplying CCD would yield even higher SNR.

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